

# Steganalysis in high dimensions: Fusing classifiers built on random subspaces

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# Motivation

- Modern steganography
  - Minimizing a distortion function in a high dimensional feature space  
Example: HUGO [Pevný-2010] (spatial domain) –  $10^7$  dimensions
  - Preserving complex models  
Example: Optimized  $\pm 1$  embedding (JPEG domain) [Filler-Yesterday]
- Modern approach to steganalysis
  - Needs to follow the suit and capture more and more statistics
  - Cartesian calibration [2009] – doubles dimensionality
  - Merging of existing features together
  - $\pm 1$  embedding  $\rightarrow$  SPAM features (686) [Pevný-2009]
  - YASS algorithm (JPEG domain)  $\rightarrow$  CDF features (1,234) [2010]

# Curse of dimensionality

- Growing complexity of training
- Limited training data / no access to the cover source
- Degradation of generalization abilities (overtraining)  
⇒ model assumptions / regularization
- Problems with data / memory management
- Saturation of performance below its potential

*Features are designed to have low dimensionality*

# Our goals

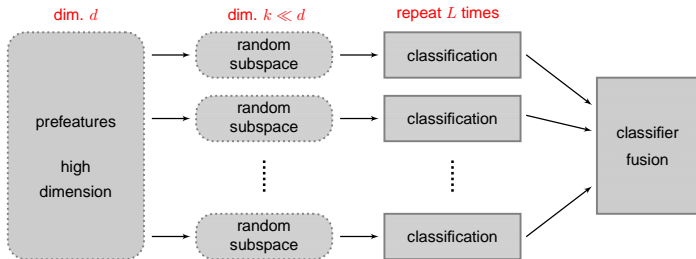
- Challenge the low-dimensional limitation for a feature design
- Replace human design of features with an automatized procedure
- Rethink machine learning approach to steganalysis
- Classify in very high dimensions with low complexity and without compromising the performance
- Improve state-of-the-art steganalysis

# What are the options?

1. Apply a classification tool of choice directly
2. Reduce dimensionality and then classify
  - Unsupervised techniques (PCA)
  - Supervised techniques (feature extraction / selection)
  - Can be thought of as part of the feature design
3. Reduce dimensionality and simultaneously classify
  - Minimize an appropriately defined objective function (SVDM)
  - Iterative process with a classification feedback (embedded methods)
4. Ensemble methods
  - Reduce dimensionality randomly and construct a simple classifier
  - Repeat  $L$  times and aggregate the individual decisions

# The proposed framework

- Step 1 – Form high-dimensional *prefeatures*
  - Capture as many dependencies among cover elements as possible
  - Don't be restricted by a dimensionality
  - Emphasize diversity of individual features
- Step 2 – Classify in high dimensions using an ensemble approach



## Specific implementation

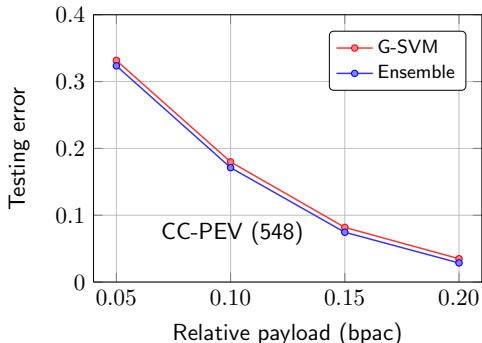
- Random subspace = random *selection* (without repetition)
  - ⇒ The complexity does not depend on the dimensionality  $d$
- Individual classifiers (base learners)
  - Need to be sufficiently diverse (need to make different errors)
  - Weak and unstable classifiers preferable
  - Our choice: Fisher Linear Discriminants (FLDs)
- Fusion = majority voting scheme  $\sum_{i=1}^L \text{decision}(i) > \text{threshold}$
- Parameters  $k \approx 300 - 3000$ ,  $L \approx 30 - 150$

Relation to previous art:

- [\[Freund-1999\]](#) – Boosting (aggregation of weak classifiers)
- [\[Breiman-2001\]](#) – Random forests (base learners = trees)

# Comparison with SVM

- JPEG domain, algorithm nsF5, database of 6500 images
- State-of-the-art feature sets
  - CC-PEV ( $2 \times 274 = 548$ ) – [Pevný-2007] + Cartesian calibration

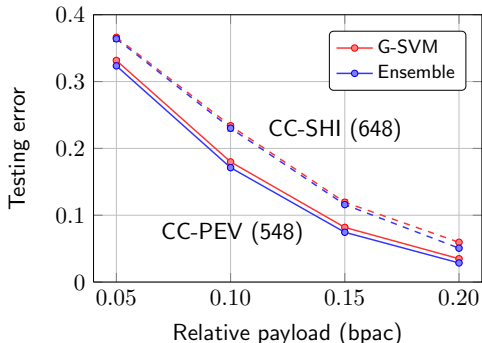


- $k = 400, L = 31$
- Ensemble: 70 sec
- G-SVM: 250 sec  
( $3.5 \times$  longer)
- Full training: 8 hrs!



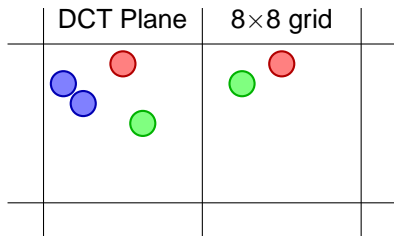
# Comparison with SVM

- JPEG domain, algorithm nsF5, database of 6500 images
- State-of-the-art feature sets
  - CC-PEV ( $2 \times 274 = 548$ ) – [Pevný-2007] + Cartesian calibration
  - CC-SHI ( $2 \times 324 = 648$ ) – [Shi-2006] + Cartesian calibration



- $k = 400, L = 31$
- Ensemble: 70 sec
- G-SVM: 250 sec  
( $3.5 \times$  longer)
- Full training: 8 hrs!

# Generating high-dimensional prefeatures (in JPEG domain)



intra-block dependencies

inter-block dependencies

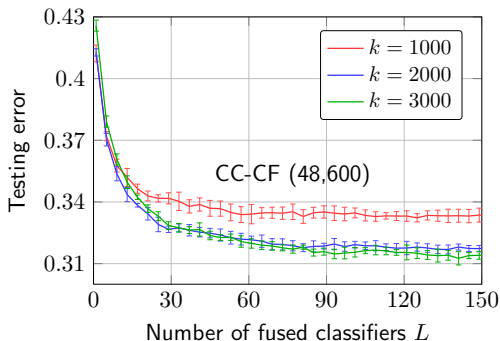
combination of both

- 2D co-occurrence matrices
- Driven by mutual information
- $N$  matrices in total
- Truncated to  $[-T, T]$
- Cartesian calibration
- Dimension  $2 \times N \times (2 \times T + 1)^2$
- $T = 4, N = 300 \rightarrow \text{dim} = 48,600$

CC-CF features

# Steganalysis of nsF5

- Influence of parameters  $L$  and  $k$

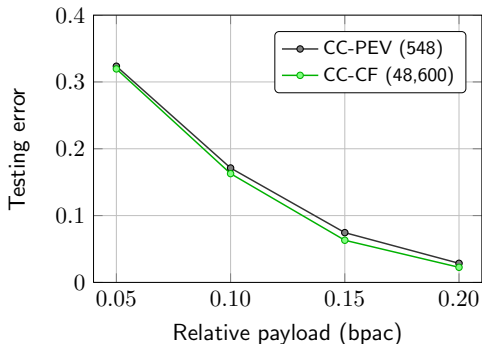


- Payload 0.05 bpac
- $k = 2000, L = 149$   
→ 30 min
- G-SVM: 7.5 hrs  
(15 × longer)  
Full training > month

- Performance quickly saturates as  $L$  grows
- Choice of  $k$  is important (1D search may be conducted)

# Steganalysis of nsF5

- Can we improve state-of-the-art?



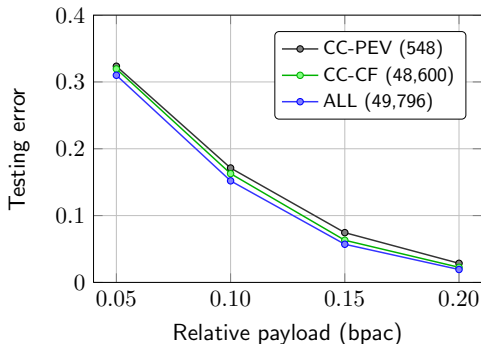
— CC-PEV: G-SVM

— Rest: Ensemble

$k = 2000, L = 149$

# Steganalysis of nsF5

- Can we improve state-of-the-art?



— CC-PEV: G-SVM

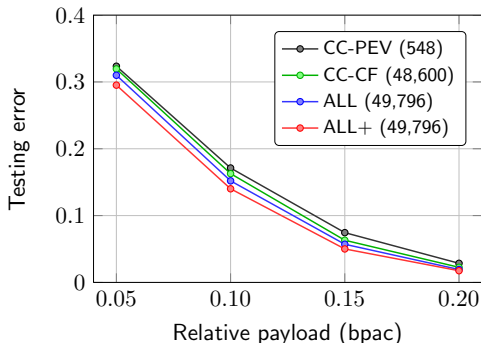
— Rest: Ensemble

$k = 2000, L = 149$

- ALL (49,796) = CC-PEV (548) + CC-SHI (648) + CC-CF (48,600)

# Steganalysis of nsF5

- Can we improve state-of-the-art?



— CC-PEV: G-SVM

— Rest: Ensemble

$k = 2000, L = 149$

- ALL (49,796) = CC-PEV (548) + CC-SHI (648) + CC-CF (48,600)
- ALL+ = ALL with 300/2000 always chosen from CC-PEV

# Generating high-dimensional prefeatures (in SPATIAL domain)

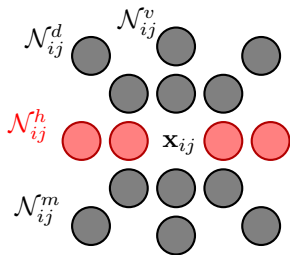
- Modeling the joint distribution of higher order local residuals
- Horizontal residual  $\mathbf{H}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^h)$



Order	$\mathbf{H}_{ij}$
2	$\frac{1}{2}(-\mathbf{x}_{i,j-1} + 2\mathbf{x}_{ij} - \mathbf{x}_{i,j+1})$
3	$\frac{1}{3}(-\mathbf{x}_{i,j-1} + 3\mathbf{x}_{ij} - 3\mathbf{x}_{i,j+1} + \mathbf{x}_{i,j+2})$
4	$\frac{1}{6}(\mathbf{x}_{i,j-2} - 4\mathbf{x}_{i,j-1} + 6\mathbf{x}_{ij} - 4\mathbf{x}_{i,j+1} + \mathbf{x}_{i,j+2})$
5	$\frac{1}{10}(\mathbf{x}_{i,j-2} - 5\mathbf{x}_{i,j-1} + 10\mathbf{x}_{i,j} - 10\mathbf{x}_{i,j+1} + 5\mathbf{x}_{i,j+2} - \mathbf{x}_{i,j+3})$
6	$\frac{1}{20}(-\mathbf{x}_{i,j-3} + 6\mathbf{x}_{i,j-2} - 15\mathbf{x}_{i,j-1} + 20\mathbf{x}_{ij} - 15\mathbf{x}_{i,j+1} + 6\mathbf{x}_{i,j+2} - \mathbf{x}_{i,j+3})$

# Generating high-dimensional prefeatures (in SPATIAL domain)

- Modeling the joint distribution of higher order local residuals
- Horizontal residual  $\mathbf{H}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^h)$



$$\mathbf{H}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^h) \quad \mathbf{D}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^d)$$

$$\mathbf{V}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^v) \quad \mathbf{M}_{ij} = \mathbf{x}_{ij} - \text{Pred}(\mathcal{N}_{ij}^m)$$

$\mathbf{H}_{ij}, \mathbf{V}_{ij}, \mathbf{D}_{ij}, \mathbf{M}_{ij} \rightarrow \text{MARKOV}$

$\min\{\mathbf{H}_{ij}, \mathbf{V}_{ij}, \mathbf{D}_{ij}, \mathbf{M}_{ij}\} \rightarrow \text{MINMAX}$

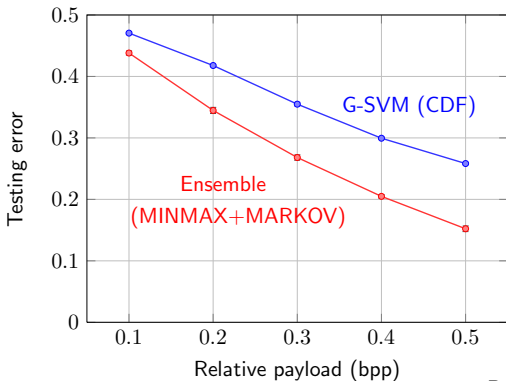
$\max\{\mathbf{H}_{ij}, \mathbf{V}_{ij}, \mathbf{D}_{ij}, \mathbf{M}_{ij}\}$

- 3D co-occurrences, dimension  $20 \times (2 \times T + 1)^3$  ( $T = 4 \rightarrow \text{dim} = 14,580$ )



# Steganalysis of HUGO

- G-SVM  $\rightarrow$  CDF (1,234) = CC-PEV (548) + SPAM (686)
- Ensemble  $\rightarrow$  MINMAX+MARKOV (14,580),  $k = 1600$ ,  $L = 51$



BOSSbase (9074 images)  
size: 512×512, resized

# Summary

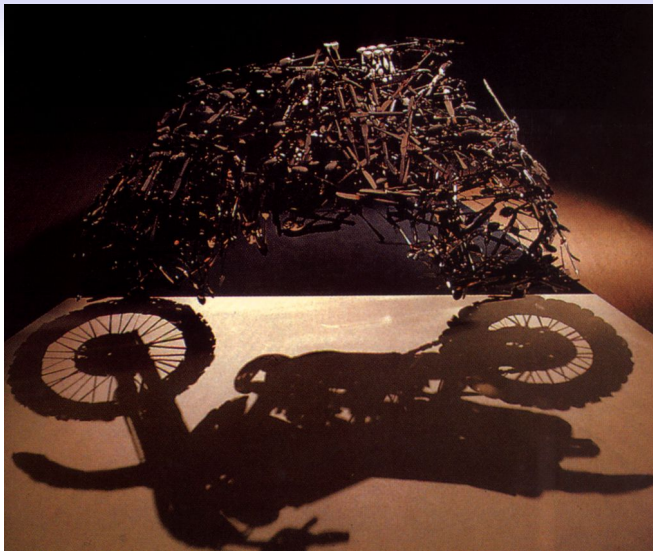
## The main contributions for future steganalysis

- High dimensionality doesn't have to be a restriction for the feature design
- Proposed scalable, fast, and simple classification methodology based on ensemble classifiers
- One step further towards automatization of steganalysis
- Showed that state-of-the-art steganalysis can be improved by a large margin

## Open problems

- How to design prefeatures?
- How to define random projections?

## The power of random projections



*Shigeo Fukuda, Lunch With a Helmet On (1987)*